

Machine Translation

CSE 447 / 517

March 3rd, 2022 (Week 9)

Logistics

- A8 due is due **tomorrow** (Friday, March 4th)

Agenda

- Beam Search
- IBM Model 1
 - EM algorithm
- IBM Model 2
- Quiz 8
- Q & A

Beam search decoding

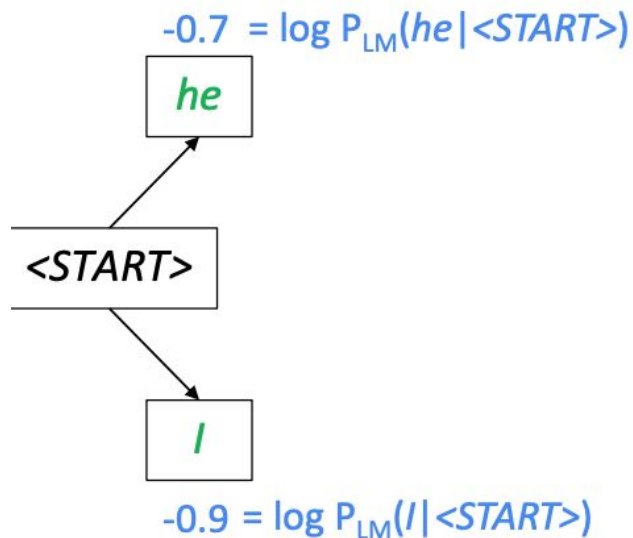
- Core idea: On each step of decoder, keep track of the ***k* most probable** partial translations (which we call ***hypotheses***)
 - *k* is the **beam size** (in practice around 5 to 10)
- A hypothesis y_1, \dots, y_t has a **score** which is its log probability:

$$\text{score}(y_1, \dots, y_t) = \log P_{\text{LM}}(y_1, \dots, y_t | x) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$$

- Scores are all negative, and higher score is better
 - We search for high-scoring hypotheses, tracking top *k* on each step
- Beam search is **not guaranteed** to find optimal solution
- But **much more efficient** than exhaustive search!

Beam search decoding: example

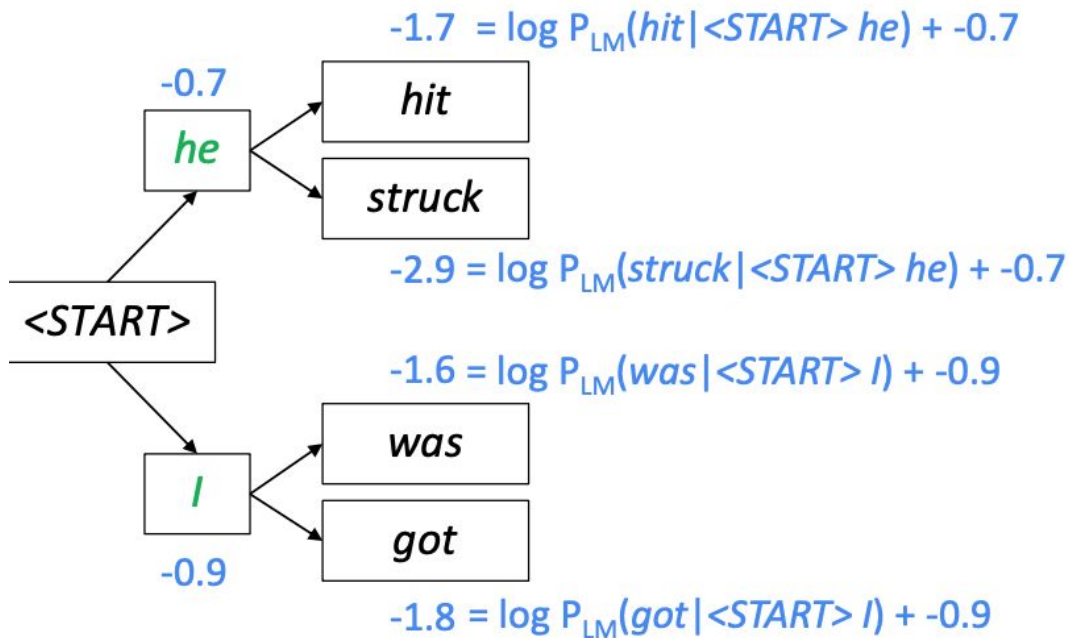
Beam size = $k = 2$. Blue numbers = $\text{score}(y_1, \dots, y_t) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$



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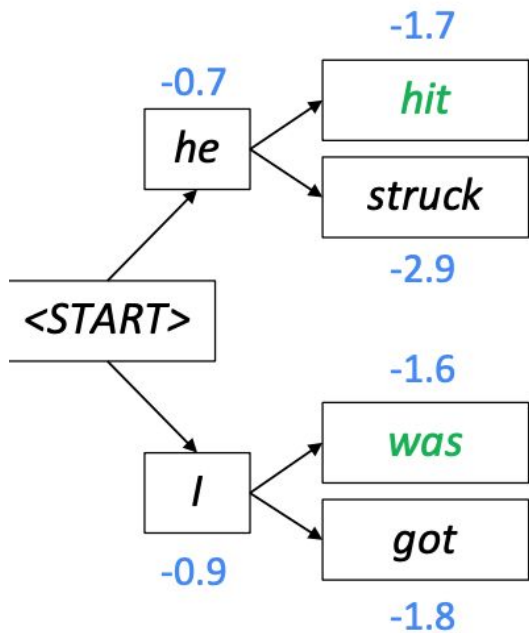
For each of the k hypotheses, find top k next words and calculate scores



Beam search decoding: example

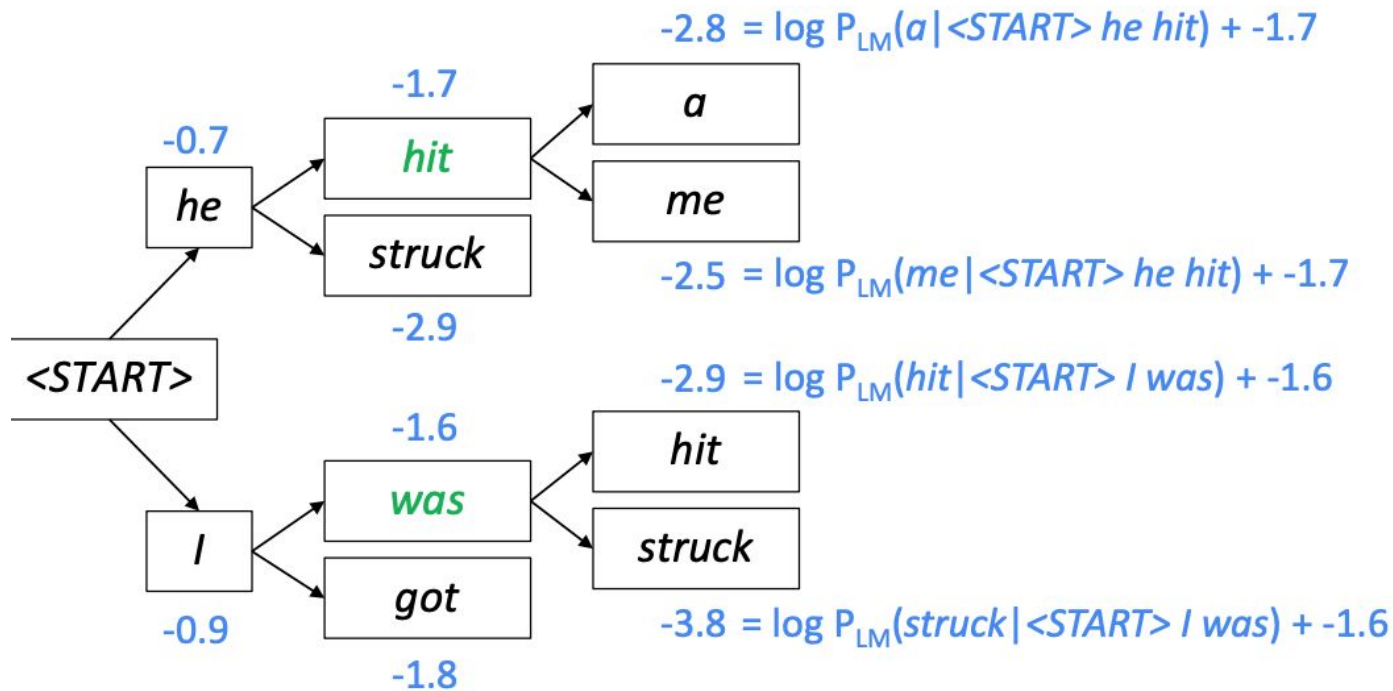
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Of these k^2 hypotheses, just keep k with highest scores



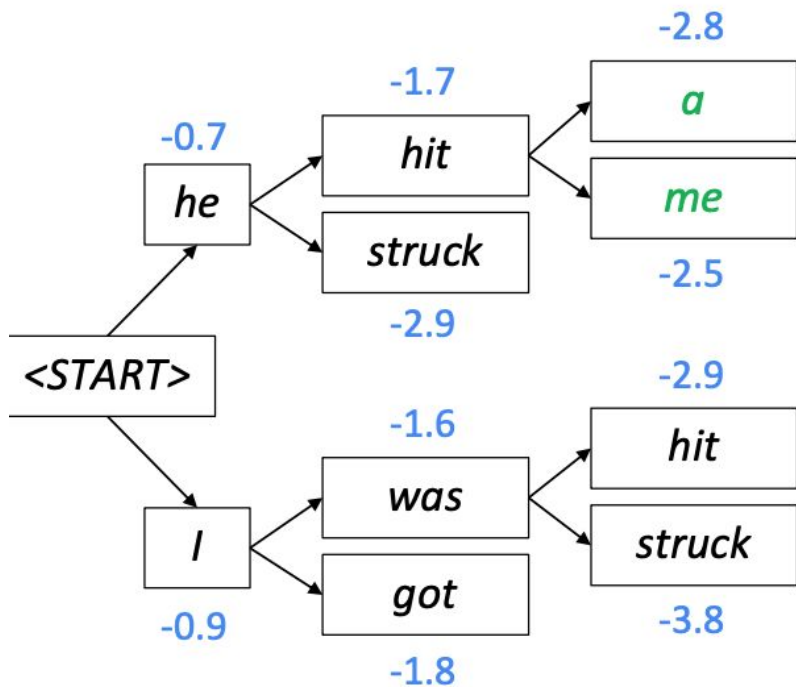
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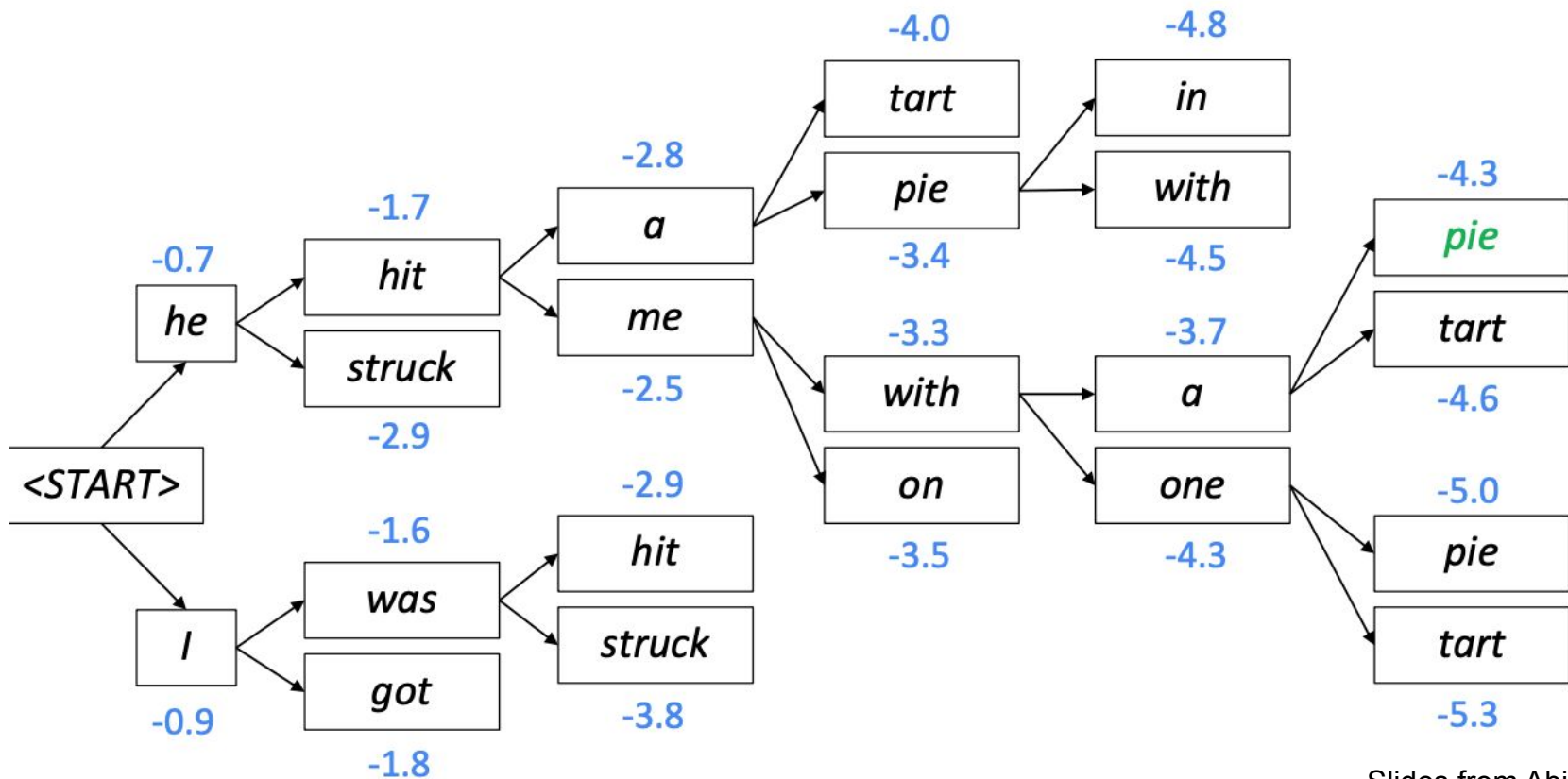
Beam search decoding: example

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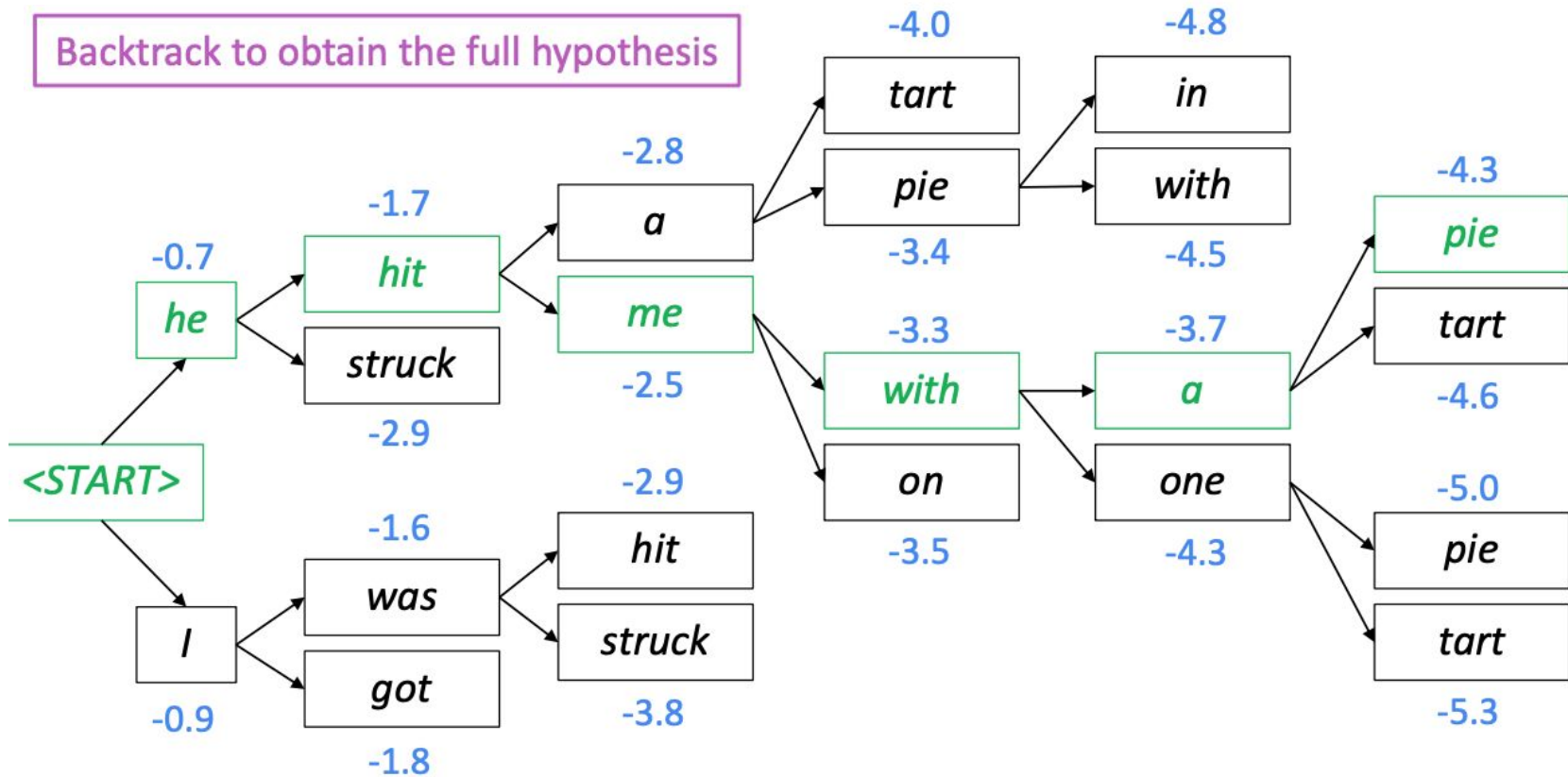
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Quiz 8: FOL

Select **all** the correct translation of following sentences into FOL using the key below:

G: ... is guilty

C: ... is a criminal

L: ... loves...

Quiz 8: FOL

Not every criminal is innocent.

$$\neg \forall x (C(x) \Rightarrow \neg G(x))$$

$$\exists x (C(x) \wedge G(x))$$

Quiz 8: FOL

Not every criminal is innocent.

$$\neg \forall x (C(x) \Rightarrow \neg G(x))$$

$$\exists x (C(x) \wedge G(x))$$

They are logically equivalent – so both is correct

Quiz 8: FOL

Nobody loves anybody who loves nobody.

$$\forall x (\forall y \neg L(x, y) \Rightarrow \forall z \neg L(z, x))$$

$$\forall x (\forall y \neg L(x, y) \Rightarrow \neg \exists z L(z, x))$$

$$\forall x (\forall y \neg L(x, y) \Rightarrow \neg \forall z L(z, x))$$

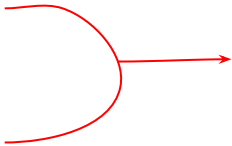
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Logically equivalent, both are correct

NLP Task: Machine Translation

Mr President , Noah's ark was filled not with production factors , but with living creatures .
(From Language X)



Noahs Arche war nicht voller Produktionsfaktoren , sondern Geschöpfe .
(To Language Y)

The Noisy Channel Model

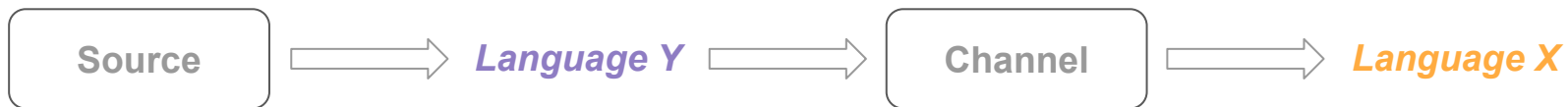
Language X  *Language Y*

We want to translate *Language X* into *Language Y*.

The Noisy Channel Model

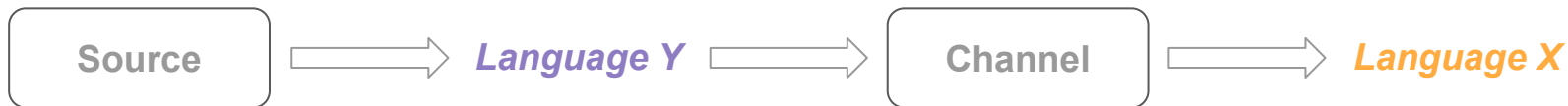
Language X \longrightarrow *Language Y*

We want to translate *Language X* into *Language Y*.



Imagine there is a source that generates *Language Y*. But then it is passed through some channel, and we observe *Language X* on the other side of the channel.

The Noisy Channel Model

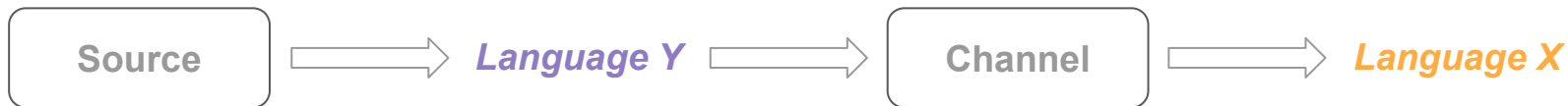


Imagine there is a source that generates *Language Y*. But then it is passed through some channel, and we observe *Language X* on the other side of the channel.

$$\begin{aligned} y^* &= \operatorname{argmax}_y p(y | x) \\ &= \operatorname{argmax}_y p(x | y) \cdot p(y) \end{aligned}$$

Source model aka a LM for Language Y! This captures the fluency in the target language.

The Noisy Channel Model

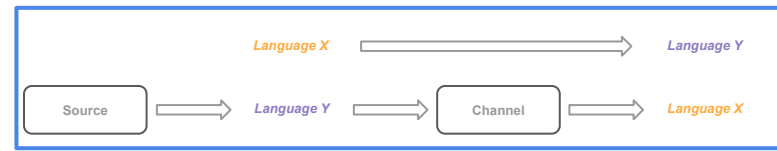


Imagine there is a source that generates *Language Y*. But then it is passed through some channel, and we observe *Language X* on the other side of the channel.

$$\begin{aligned} y^* &= \operatorname{argmax}_y p(y | x) \\ &= \operatorname{argmax}_y p(x | y) \cdot p(y) \end{aligned}$$

Channel model, captures the faithfulness of the translation.

The Noisy Channel Model

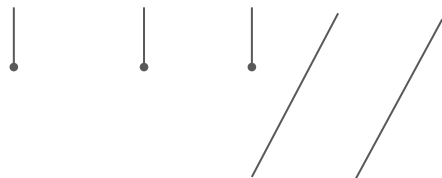


Refer to this when you get lost which is which!

IBM Model 1 - Motivation



Mr President , Noah's ark was filled not with production factors , but with living creatures .



Noahs Arche war nicht voller Produktionsfaktoren , sondern Geschöpfe .

.....

IBM Model 1: What is the mapping from each token in *Language X* to *Language Y*?

IBM Model 1 - Alignment



IBM Model 1: What is the mapping from each token in *Language X* to *Language Y*?

Let l be the length of y and m be the length of x .

Latent variable $a = \langle a_1, \dots, a_m \rangle$, each a_i ranging over $\{0, \dots, l\}$ (positions in y).

$$a_i = j$$

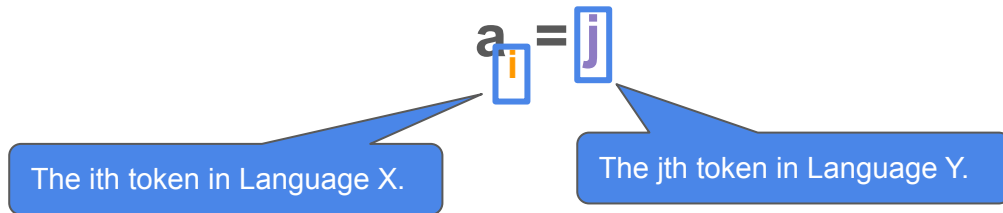
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IBM Model 1: What is the mapping from each token in *Language X* to *Language Y*?

$$a = [0, 0, 0, 1, \quad ??? \quad]$$

IBM Model 1



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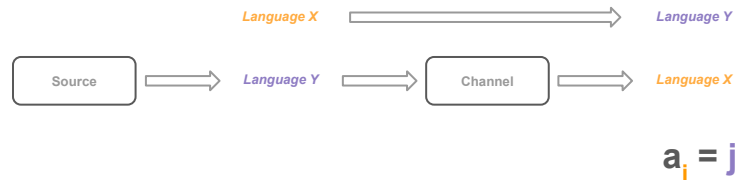


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IBM Model 1: What is the mapping from each token in *Language X* to *Language Y*?

$$a = [0, 0, 0, 1, 2, 3, 5, 4, 0, 6, 6, 7, 8, 0, 0, 9, 10]$$

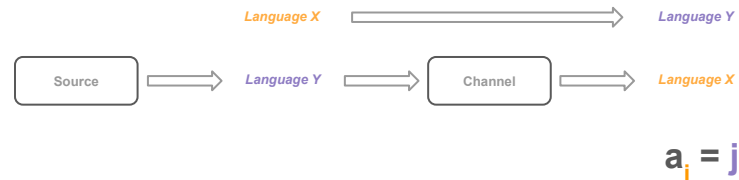
IBM Model 1



Our channel model:

$$p(\mathbf{x} | \mathbf{y}, m; \theta) = \sum_{\mathbf{a} \in \{0, \dots, l\}^m} p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta)$$

IBM Model 1



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Marginalized over all possible \mathbf{a} vectors.

IBM Model 1



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where

$$\begin{aligned} p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) &= \prod_{i=0}^m p(a_i | i, l, m) \cdot p(x_i | y_{a_i}; \theta) \\ &= \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}} \end{aligned}$$

IBM Model 1



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Go through every position in \mathbf{x} .

where

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How likely is the current alignment *without* regard to the text?

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$$= \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}}$$

Uniform distribution (all distortions modelled by \mathbf{a} are treated the same).

IBM Model 1



$$a_i = j$$

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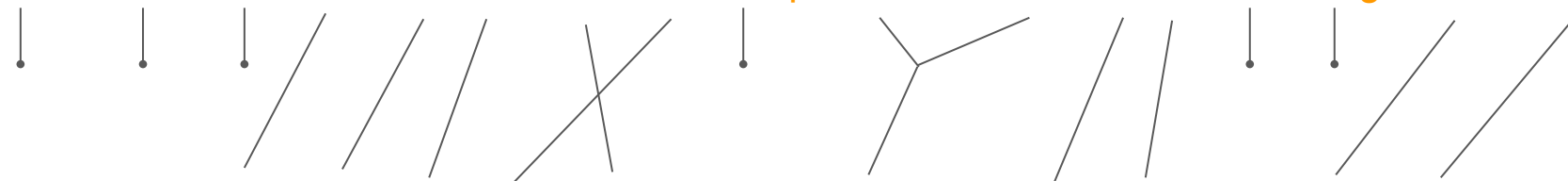
Learned parameter.

IBM Model 1



$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}}$$

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Noahs Arche war nicht voller Produktionsfaktoren , sondern Geschöpfe .

$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \frac{1}{1+10} \cdot \theta_{Mr | null} + \dots$$

IBM Model 1 - Learning



$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}}$$

IBM Model 1 - Learning



$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}}$$

How do we estimate this?

IBM Model 1 - Learning

$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}}$$



The problem: we don't know the alignments ahead of time. So we can't apply MLE to find the parameter.

The solution: expectation maximization.

Expectation Maximization

Goal: finding $\theta_{x_i|y_{a_i}}$.

Step 1: initialize $\theta_{x_i|y_{a_i}}$ with some value.

Step 2: use $\theta_{x_i|y_{a_i}}$ to estimate “soft” alignments.

Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.

Step 4: repeat from 2!



Expectation Maximization

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Expectation Maximization



Step 2: use $\theta_{x_i|y_{a_i}}$ to estimate “soft” alignments: $q_i(j) = p(a_i = j; \theta)$.

$$q_i(j) \leftarrow \frac{\theta_{x_i|y_j}}{\sum_{j'=1}^l \theta_{x_i|y_{j'}}$$

Expectation Maximization



Step 2: use $\theta_{x_i|y_{a_i}}$ to estimate “soft” alignments: $q_i(j) = p(a_i = j; \theta)$.

What is the likelihood of generating x_i given the y_j ?

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Expectation Maximization



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What is the likelihood of generating x_i given the y_j ?

$$q_i(j) \leftarrow \frac{\theta_{x_i|y_j}}{\sum_{j'=1}^l \theta_{x_i|y_{j'}}$$

... out of all possible $y_{j'}$ that x_i could be aligned to.

Expectation Maximization



Step 2: use $\theta_{x_i|y_{a_i}}$ to estimate “soft” alignments: $q_i(j) = p(a_i = j; \theta)$.

We want a soft assignment for each sample n .

$$q_i^{(n)}(j) \leftarrow \frac{\theta_{x_i^{(n)}|y_j^{(n)}}}{\sum_{j'=1}^l \theta_{x_i^{(n)}|y_{j'}^{(n)}}$$

Expectation Maximization



Step 2: use $\theta_{x_i|y_{a_i}}$ to estimate “soft” alignments: $q_i(j) = p(a_i = j; \theta)$.

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Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.

Step 4: repeat from 2!



Expectation Maximization

Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.



$$\hat{\theta}_{x|y} \leftarrow \frac{\sum_{n=1}^N \sum_{i: x_i^{(n)}=x} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}{\sum_{n=1}^N \sum_{i=1}^{m^{(n)}} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}$$

Expectation Maximization



Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.

Go through all samples in the dataset.

$$\hat{\theta}_{x|y} \leftarrow \frac{\sum_{n=1}^N \sum_{i: x_i^{(n)}=x} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}{\sum_{n=1}^N \sum_{i=1}^{m^{(n)}} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}$$

Expectation Maximization



Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.

Go through each position i that token x appeared.

$$\hat{\theta}_{x|y} \leftarrow \frac{\sum_{n=1}^N \sum_{i: x_i^{(n)}=x} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}{\sum_{n=1}^N \sum_{i=1}^{m^{(n)}} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}$$

Expectation Maximization



Step 3: estimate $\theta_{x_i|y_{a_i}}$ with MLE principle.

How much of the probability mass is assigned to i matching j ?

$$\hat{\theta}_{x_i|y} \leftarrow \frac{\sum_{n=1}^N \sum_{i: x_i^{(n)}=x} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}{\sum_{n=1}^N \sum_{i=1}^{m^{(n)}} \sum_{j: y_j^{(n)}=y} q_i^{(n)}(j)}$$

Expectation Maximization



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Go through all samples in the dataset.

Expectation Maximization



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Expectation Maximization



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How much probability mass is assigned to the word x matching y?

Expectation Maximization

Goal: finding $\theta_{x_i|y_{a_i}}$.

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Step 4: repeat from 2!



IBM Model 2

Recall IBM Model 1:

$$\begin{aligned} p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) &= \prod_{i=0}^m p(a_i | i, l, m) \cdot p(x_i | y_{a_i}; \theta) \\ &= \prod_{i=0}^m \frac{1}{l+1} \cdot \theta_{x_i | y_{a_i}} \end{aligned}$$



IBM Model 2



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IBM Model 2: removed uniform distortion assumption.

$$p(\mathbf{x}, \mathbf{a} | \mathbf{y}, m; \theta) = \prod_{i=0}^m = \theta_{a_i | i, l, m}^{distortion} \cdot \theta_{x_i | y_{a_i}}^{translation}$$

Q & A